Diffractive photoproduction of dijets in ep collisions at HERA

The ZEUS Collaboration

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Abstract. Diffractive photoproduction of dijets was measured with the ZEUS detector at the ep collider HERA using an integrated luminosity of $77.2\,\mathrm{pb}^{-1}$. The measurements were made in the kinematic range $Q^2 < 1\,\mathrm{GeV}^2$, 0.20 < y < 0.85 and $x_{IP} < 0.025$, where Q^2 is the photon virtuality, y is the inelasticity and x_{IP} is the fraction of the proton momentum taken by the diffractive exchange. The two jets with the highest transverse energy, $E_{\mathrm{T}}^{\mathrm{jet}}$, were required to satisfy $E_{\mathrm{T}}^{\mathrm{jet}} > 7.5$ and 6.5 GeV, respectively, and to lie in the pseudorapidity range $-1.5 < \eta^{\mathrm{jet}} < 1.5$. Differential cross sections were compared to perturbative QCD calculations using available parameterisations of diffractive parton distributions of the proton.

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1 Introduction

In diffractive electron–proton scattering, the proton loses a small fraction of its energy and either emerges from the scattering intact, $ep \to eXp$, or dissociates into a low-mass state $N, ep \to eXN$. A large rapidity gap (LRG) separates the hadronic system X with invariant mass M_X and the final-state proton p.

In the framework of Regge phenomenology [1-3], diffractive interactions are ascribed to the exchange of

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a trajectory with vacuum quantum numbers, the pomeron trajectory. In quantum chromodynamics (QCD), the diffractive factorisation theorem [4–7] states that the diffractive cross section in deep inleastic scattering (DIS) can be expressed as the convolution of universal partonic cross sections and a specific type of parton distribution functions (PDF), the diffractive PDF (dPDF). Diffractive PDFs are interpreted as the number density of partons conditional on the observation of a diffracted proton in the final state. The dPDFs [8–11] have been determined from the HERA inclusive measurements of the diffractive structure function $F_2^{\rm D}$ [8, 9], defined in analogy with the proton structure function F_2 , and were used for input to calculations of hard diffractive processes at HERA, Tevatron and LHC [12–20].

Diffractive collisions producing a state X with a dijet system are a particularly interesting component of diffractive ep interactions. The transverse energies of the jets provide a hard scale, ensuring the applicability of perturbative QCD at the small photon virtualities considered here. In photoproduction, at leading order (LO) of QCD, two types of processes contribute to dijet photoproduction, namely direct and resolved photon processes. In direct photon processes, the exchanged photon participates as a point-like particle, interacting with a gluon from the incoming proton (photon-gluon fusion, Fig. 1a). Thus, these processes are directly sensitive to the gluon content of the diffractive exchange. In resolved photon processes, the photon behaves as a source of partons, one of which interacts with a parton from the diffractive exchange (Fig. 1b). For resolved photon processes, which resemble hadronhadron interactions, QCD factorisation is not expected to hold [6, 7, 21-23]. Further interactions between partons from the photon and the proton may fill the rapidity gap, leading to a breakdown of hard-scattering factorisation and causing a suppression of the diffractive photoproduction cross section. Such a mechanism was proposed to explain the suppression of the measured cross sections for hard diffractive hadron-hadron scattering at the tevatron with respect to expectations based on dPDFs obtained at HERA [24]. For the diffractive resolved photoproduction, an eikonal model [25, 26] predicts a cross-section suppression by about a factor of three. In the framework of another model [27], assuming that diffractive collisions reflect the absorption of an incident particle-wave, it has been argued that the strong factorisation breaking observed in diffractive hadron-induced processes should not be seen in photon-induced processes.

This analysis presents measurements of the diffractive photoproduction of dijets using the ZEUS detector at HERA. A 30-fold increase in luminosity was achieved compared to the previous ZEUS analysis [28]. This, in combination with the addition of a new forward¹ detector, allows measurements to be made in a wider kinematic range. Differential cross sections based on these measure-

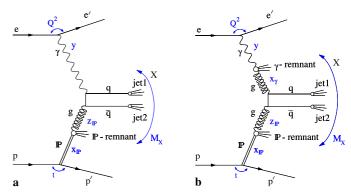


Fig. 1. Leading-order diagrams for ${\bf a}$ direct and ${\bf b}$ resolved processes in diffractive photoproduction of dijets at HERA. The variables shown in the plots are described in the text

ments are compared to next-to-leading-order (NLO) QCD predictions at the hadron level. The comparisons are also made separately for subsamples enriched with direct and resolved photoproduction. A similar study has been recently published by the H1 Collaboration [13].

2 Experimental set-up

This measurement is based on the data taken with the ZEUS detector at the ep collider HERA in 1999–2000 when electrons or positrons of 27.5 GeV were collided with protons of 920 GeV. The sample used for this study corresponds to an integrated luminosity $\mathcal{L}=77.2\,\mathrm{pb^{-1}}$ (12.1 $\mathrm{pb^{-1}}$ and 65.1 $\mathrm{pb^{-1}}$ for the e^-p and e^+p samples, respectively). A detailed description of the ZEUS detector can be found elsewhere [29]. A brief outline of the components that are most relevant for this analysis is given below.

Charged particles are tracked in the central tracking detector (CTD) [30–32], which operates in a magnetic field of 1.43 T provided by a thin superconducting coil. The CTD consists of 72 cylindrical drift chamber layers, organised in 9 superlayers covering the polar-angle region 15° < θ < 164°. The transverse-momentum resolution for full-length tracks is $\sigma(p_{\rm T})/p_{\rm T} = 0.0058 p_{\rm T} \oplus 0.0065 \oplus 0.0014/p_{\rm T}$, with $p_{\rm T}$ in GeV.

The high-resolution uranium-scintillator calorimeter (CAL) [33–36] consists of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. Each part is subdivided transversely into towers and longitudinally into one electromagnetic section (EMC) and either one (in RCAL) or two (in BCAL and FCAL) hadronic sections (HAC). The smallest subdivision of the calorimeter is called a cell. The CAL energy resolutions, as measured under test beam conditions, are $\sigma(E)/E=0.18/\sqrt{E}$ for electrons and $\sigma(E)/E=0.35/\sqrt{E}$ for hadrons, with E in GeV.

In 1998, the forward plug calorimeter (FPC) [37] was installed in the $20 \times 20 \text{ cm}^2$ beam hole of the FCAL, with a small hole of radius 3.15 cm in the centre to accommodate

 $^{^{1}}$ The ZEUS coordinate system is a right-handed Cartesian system, with the Z axis pointing in the proton beam direction, referred to as the "forward direction", and the X axis pointing left towards the centre of HERA. The coordinate origin is at the nominal interaction point.

² From now on, the word "electron" will be used as a generic term for both electron and positron.

the beam pipe. The FPC increased the forward calorimetric coverage by about one unit in pseudorapidity to $\eta \lesssim 5$.

The backing calorimeter (BAC) consists of proportional tube chambers placed in the gap of the iron yoke. In the present analysis it was used in conjunction with the CTD and the CAL to identify cosmic muons that traversed the yoke.

The luminosity was measured from the rate of the bremsstrahlung process $ep \rightarrow e\gamma p$. The resulting small-angle energetic photons were measured by the luminosity monitor [38–40], a lead-scintillator calorimeter placed in the HERA tunnel at $Z=-107\,\mathrm{m}$.

3 Kinematics and reconstruction of variables

Diffractive photoproduction in ep scattering (Fig. 1),

$$e(e) + p(p) \rightarrow e(e') + X(X) + p(p')$$
,

is described in terms of the four-momenta of the incoming and scattered electrons, e and e', of the incoming and scattered protons, p and p', and of the hadronic system, X. The following kinematic variables are defined: the photon virtuality, $Q^2 = -q^2$, where q = e - e', the squared photon-proton centre-of-mass energy, $W^2 = (p+q)^2$, and the fraction of the electron energy transferred to the proton in its rest frame (inelasticity),

$$y = \frac{p \cdot q}{p \cdot e} \simeq \frac{W^2}{2p \cdot e}$$
.

The reaction can be considered to proceed through the interaction of the virtual photon with the diffractive exchange (pomeron, IP). This process is described by the invariant mass, M_X , of the hadronic system X and the

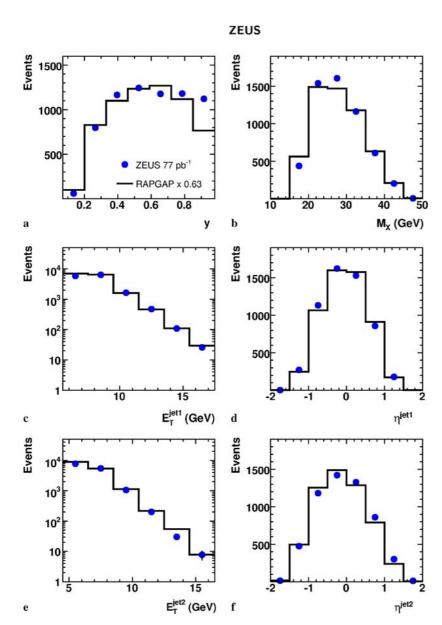


Fig. 2. Comparison of the data (*dots*) with the RAPGAP MC (*solid line*) normalised to the data as a function of a y, b M_X , c $E_{\rm T}^{\rm jet1}$, d $\eta^{\rm jet1}$, e $E_{\rm T}^{\rm jet2}$ and f $\eta^{\rm jet2}$ after all cuts but the one on the plotted variable

fraction of the proton momentum carried by the diffractive exchange $\,$

$$x_{IP} = \frac{(p - p') \cdot q}{p \cdot q} .$$

In the present data, the state X contains a dijet system as the result of a hard scattering process. The partons from the resolved photon and the diffractive exchange participating in the interaction have fractional momenta given

$$x_{\gamma} = \frac{p \cdot u}{p \cdot q} \,,$$

where u is the four-momentum of the parton in the resolved photon, and

$$z_{IP} = \frac{v \cdot q}{(p - p') \cdot q} \,,$$

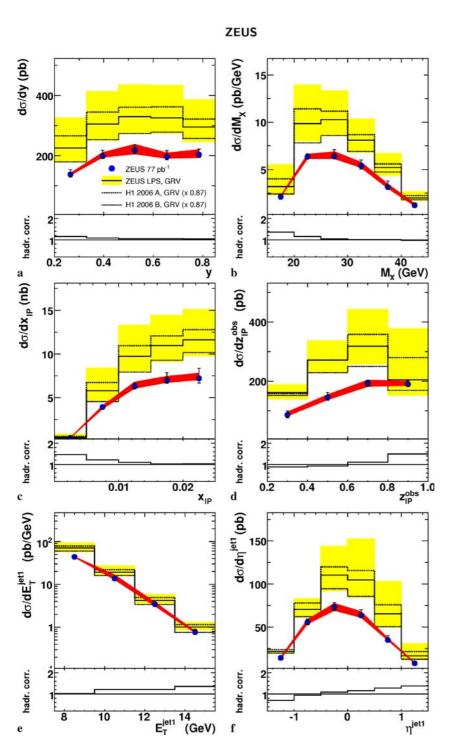


Fig. 3. Single-differential cross sections (dots) as a function of **a** y, **b** M_X , **c** x_{IP} , **d** z_{IP}^{obs} , **e** $E_{\mathrm{T}}^{\text{jet1}}$ and **f** η^{jet1} compared with NLO QCD predictions, corrected for hadronisation, using the dPDFs from the ZEUS LPS fit (solid line), the H1 2006 fit A (dashed line) and the H1 2006 fit B (dotted line) and the GRV γ -PDFs. The inner error bars of the dots show the statistical uncertainty, the outer error bars show the statistical and systematic uncertainties (see Sect. 7) added in quadrature. The dark shaded band indicates the jet energy scale uncertainty. The $light\ shaded\ band\ shows\ the\ theoretical\ un$ certainty due to the variation of the scale when using the ZEUS LPS fit. Underneath each plot the hadronisation corrections applied to the NLO prediction at parton level are shown

where v is the four-momentum of the parton in the diffractive exchange.

Energy flow objects (EFOs) were reconstructed from CAL clusters and CTD tracks and combine the CTD and CAL information to optimise the resolution of the reconstructed kinematic variables [41,42]. The EFOs were additionally corrected for energy loss due to inactive material in front of the CAL [43].

The mass M_X of the hadronic system X was reconstructed as

$$M_X = \sqrt{\sum_h (E - p_Z)_h \cdot \sum_h (E + p_Z)_h} ,$$

where the index h runs over all EFOs. The quantities E and p_Z indicate the energy and the longitudinal momentum of the EFOs, respectively.

The inelasticity, y, was estimated from the EFOs according to the Jacquet–Blondel method [44] as

$$y_{\rm JB} = \sum_h \left(E - p_Z\right)_h / 2E_e \,, \label{eq:JB}$$

where E_e is the initial electron energy. For events with an electron candidate, the inelasticity was also determined from the scattered electron, y_e .

The longitudinal momentum fraction transferred from the proton to the diffractive exchange, x_{IP} , was reconstructed as

$$x_{IP} = \sum_{h} (E + p_Z)_h / 2E_p \,,$$

where E_p is the initial proton energy.

The jets were reconstructed from the EFOs by using the $k_{\rm T}$ algorithm [45] in the longitudinally inclusive mode [46] in the laboratory frame. The variables $E_{\rm T}^{\rm jet1,2}$ and $\eta^{\rm jet1,2}$ characterise the two jets with highest transverse energy, $E_{\rm T}$, with $E_{\rm T}^{\rm jet1} > E_{\rm T}^{\rm jet2}$. For the variables x_{γ} and $z_{I\!\!P}$, which are not measurable directly, the observable estimators $x_{\gamma}^{\rm obs}$ [47] and $z_{I\!\!P}^{\rm obs}$ were reconstructed as

$$\begin{split} x_{\gamma}^{\text{obs}} &= \frac{\sum_{\text{jet1,2}} E_{\text{T}}^{\text{jet}} e^{-\eta^{\text{jet}}}}{2y E_e} \,, \\ z_{IP}^{\text{obs}} &= \frac{\sum_{\text{jet1,2}} E_{\text{T}}^{\text{jet}} e^{\eta^{\text{jet}}}}{2x_{IP} E_p} \,, \end{split}$$

where the sums run over the two highest $E_{\rm T}$ jets.

In direct-photon processes, at LO in QCD, x_{γ} is equal to one, whereas resolved-photon processes appear at $x_{\gamma} < 1$. A direct-enriched region was defined by $x_{\gamma}^{\text{obs}} \geq 0.75$ and a resolved-enriched region by $x_{\gamma}^{\text{obs}} < 0.75$.

4 Event selection

A three-level trigger system was used to select events online [29, 48, 49]. Events with a large energy deposit in the calorimeter, neglecting the three inner rings of cells around the beampipe in the FCAL, were selected at the first-level trigger. Additional cuts were applied at the second-level trigger to reject beam-gas interactions and other non-ep background events. At the third level, the measured transverse energy, excluding the first inner ring of the FCAL, was required to be greater than 11 GeV. Jets were not preselected at any trigger level.

Well-reconstructed events were selected by applying the following quality cuts. The events were required to have at least three well-measured tracks of transverse momentum $p_{\rm T} > 0.2$ GeV originating from the same vertex. The longitudinal position of the vertex, $Z_{\rm vtx}$, had to be in the range $-35~{\rm cm} < Z_{\rm vtx} < 30~{\rm cm}$.

Photoproduction events were selected as follows. Events with a scattered electron candidate having an inelasticity of $y_e \leq 0.7$ were assumed to be DIS events and removed. In addition, $0.20 < y_{\text{JB}} < 0.85$ was required. The cut on

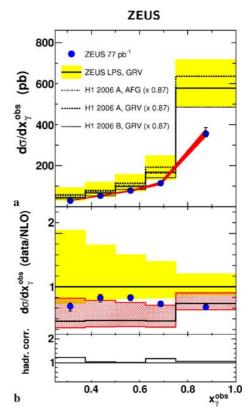


Fig. 4. a Single-differential cross section as a function of $x_{\gamma}^{\rm obs}$ compared with NLO QCD predictions, corrected for hadronisation, using the dPDFs from the ZEUS LPS fit (solid line), the H1 2006 fit A (dashed line) and the H1 2006 fit B (dotted line) and the GRV γ -dPDF. The prediction with H1 2006 fit A is also shown using the AFG parametrisation of the γ -PDFs (dashed-dotted line). Other details are the same as in the caption of Fig. 3. b Ratio of data and NLO predictions using the ZEUS LPS fit and GRV. The histogram indicates the expectation with the predicted resolved photon component scaled down by a factor of 0.34. The shaded and hatched bands show the theoretical uncertainty. Underneath the hadronisation corrections applied to the NLO prediction at parton level are shown

 y_e and the upper cut on y_{JB} reduced the remaining background from DIS events and also restricted the range of the virtuality of the exchanged photon to $Q^2 < 1 \text{ GeV}^2$ with a median value of 10^{-3} GeV^2 . The lower cut on y_{JB} removed proton-beam gas events which deposit energy in the FCAL near the beam pipe.

Events with at least two jets were selected by requiring a transverse jet energy above $E_{\rm T}^{\rm jet1(2)} > 7.5~(6.5)$ GeV. Both jets were required to be in the pseudorapidity range $-1.5 < \eta^{\rm jet1,2} < 1.5$, measured in the laboratory frame.

Diffractive events were selected by requiring the presence of a LRG between the scattered proton and the rest of the hadronic final state. Since the proton was not measured, the requirement of a LRG was implemented by a cut on the total energy in the FPC, $E_{\rm FPC} < 1.0$ GeV, and by demanding $\eta_{\rm max} < 2.8$. Here $\eta_{\rm max}$ is defined as the pseudorapidity of the most forward EFO with an energy above

400 MeV in the CAL. This selection ensures at least a twounit rapidity gap in the hadronic system, suppressing background from non-diffractive and proton-dissociative processes. In addition, a cut $x_{IP} < 0.025$ was applied to enhance the pomeron-exchange contribution [50].

Finally, cosmic-ray events originating from muons that traversed the detector near the interaction point were removed. Details can be found elsewhere [51,52]. A total of 6990 events remained after all selection cuts.

5 Monte Carlo simulations

Monte Carlo (MC) simulations were used to determine acceptances and resolution effects at detector level and to extract the hadronisation corrections for the NLO predic-

Table 1. Differential cross sections for the diffractive photoproduction of dijets as a function of y, M_X , $x_{I\!P}$ and $z_{I\!P}^{\rm obs}$ listed with statistical ($\delta_{\rm stat}$) and systematic ($\delta_{\rm syst}$) uncertainties and energy scale ($\delta_{\rm ES}$) uncertainties; the last column shows the hadronisation corrections ($C_{\rm had}$) applied to the NLO QCD predictions

y bin	$\frac{\mathrm{d}\sigma/\mathrm{d}y}{\mathrm{(pb)}}$	$\delta_{ m stat} \ m (pb)$	$\delta_{ m syst} \ m (pb)$	$\delta_{ m ES} \ m (pb)$	C_{had}
0.20, 0.33	137.9	5.3	$^{+15.2}_{-7.0}$	$^{+4.0}_{-2.9}$	1.16
0.33, 0.46	198.4	6.3	$^{+18.9}_{-5.0}$	$^{+12.1}_{-4.1}$	1.09
0.46, 0.59	218.3	6.7	$^{+16.5}_{-10.4}$	$^{+19.4}_{-12.8}$	1.05
0.59, 0.72	196.5	6.2	$+19.1 \\ -8.2$	$^{+13.0}_{-5.7}$	1.05
0.72, 0.85	203.6	6.4	$^{+17.1}_{-6.6}$	$^{+16.6}_{-10.4}$	1.04
M_X bin (GeV)	$\mathrm{d}\sigma/\mathrm{d}M_X$ (pb/GeV)	$\delta_{ m stat} \ m (pb/GeV)$	$\delta_{ m syst} \ m (pb/GeV)$	$\delta_{ m ES} \ m (pb/GeV)$	$C_{ m had}$
15.0, 20.0	2.11	0.11	$^{+0.11}_{>-0.01}$	$^{+0.13}_{>-0.01}$	1.37
20.0, 25.0	6.35	0.17	$^{+0.24}_{-0.13}$	$^{+0.26}_{-0.23}$	1.16
25.0, 30.0	6.39	0.17	$^{+0.68}_{-0.15}$	$^{+0.51}_{-0.26}$	1.04
30.0, 35.0	5.41	0.17	$+0.57 \\ -0.32$	$^{+0.36}_{-0.21}$	1.01
35.0, 40.0	3.14	0.14	$^{+0.62}_{-0.19}$	$^{+0.32}_{-0.13}$	1.01
40.0, 45.0	1.21	0.09	$^{+0.23}_{-0.08}$	$^{+0.21}_{-0.07}$	0.97
x_{IP} bin	$\mathrm{d}\sigma/\mathrm{d}x_{IP}$ (nb)	$\delta_{ m stat} \ m (nb)$	$\delta_{ m syst} \ m (nb)$	$\delta_{ m ES} \ m (nb)$	$C_{ m had}$
0.000, 0.005	0.40	0.06	$^{+0.01}_{-0.04}$	$^{+0.04}_{>-0.01}$	1.46
0.005, 0.010	3.94	0.14	$^{+0.18}_{-0.10}$	$^{+0.14}_{-0.21}$	1.21
0.010, 0.015	6.28	0.17	$^{+0.36}_{-0.10}$	$^{+0.53}_{-0.20}$	1.10
0.015, 0.020	7.00	0.19	$^{+0.84}_{-0.31}$	$^{+0.47}_{-0.27}$	1.02
0.020, 0.025	7.21	0.21	$^{+1.13}_{-0.50}$	$+0.62 \\ -0.18$	1.03
$z_{I\!P}^{ m obs}$ bin	$\mathrm{d}\sigma/\mathrm{d}z_{I\!P}^{\mathrm{obs}}$ (pb)	$\delta_{ m stat} \ m (pb)$	$\delta_{ m syst} \ m (pb)$	$\delta_{ m ES} \ m (pb)$	$C_{ m had}$
0.2, 0.4	86.4	5.0	+12.4 -9.0	+9.9 -3.6	0.88
0.4, 0.6	145.7	4.9	$^{+15.7}_{-8.9}$	$^{+9.3}_{-8.2}$	0.92
0.6, 0.8	192.9	4.9	$^{+9.6}_{-8.0}$	$^{+11.3}_{-10.7}$	1.11
0.8, 1.0	190.2	4.2	$^{+11.2}_{-0.2}$	$^{+10.8}_{-5.2}$	1.49

Table 2. Differential cross sections for the diffractive photoproduction of dijets as a function of $E_{\rm T}^{\rm jet1}$ and $\eta^{\rm jet1}$ listed with statistical ($\delta_{\rm stat}$) and systematic ($\delta_{\rm syst}$) uncertainties and energy scale ($\delta_{\rm ES}$) uncertainties; the last column shows the hadronisation corrections ($C_{\rm had}$) applied to the NLO QCD predictions

$E_{\mathrm{T}}^{\mathrm{jet1}}$ bin (GeV)	$rac{\mathrm{d}\sigma/\mathrm{d}E_{\mathrm{T}}^{\mathrm{jet}1}}{\mathrm{(pb/GeV)}}$	$\delta_{ m stat} \ ({ m pb/GeV})$	$\delta_{ m syst} \ ({ m pb/GeV})$	$\delta_{ m ES} \ m (pb/GeV)$	C_{had}
7.5, 9.5	44.0	0.8	$+3.9 \\ -1.6$	$^{+0.4}_{-1.0}$	1.02
9.5, 11.5	13.7	0.4	$^{+1.3}_{-0.5}$	$^{+3.1}_{-0.7}$	1.22
11.5, 13.5	3.5	0.2	$^{+0.3}_{-0.2}$	$^{+0.4}_{-0.3}$	1.22
13.5, 15.5	0.8	0.1	$^{+0.1}_{-0.0}$	$^{+0.1}_{-0.1}$	1.35
$\eta^{ m jet1}$ bin	$\mathrm{d}\sigma/\mathrm{d}\eta^{\mathrm{jet1}} \ \mathrm{(pb)}$	$\delta_{ m stat} \ m (pb)$	$\delta_{ m syst} \ m (pb)$	$\delta_{\mathrm{ES}} \ \mathrm{(pb)}$	$C_{ m had}$
-1.5, -1.0	14.2	0.9	$^{+1.5}_{-0.6}$	$^{+1.0}_{-1.0}$	0.70
-1.0, -0.5	55.6	1.8	$+3.1 \\ -2.4$	$+3.2 \\ -1.9$	0.94
-0.5, 0.0	72.9	2.0	$+5.0 \\ -3.6$	$+4.7 \\ -3.7$	1.09
0.0, 0.5	63.6	1.8	$^{+6.3}_{-2.2}$	$^{+4.5}_{-2.6}$	1.16
0.5, 1.0	34.9	1.3	$^{+4.9}_{-0.8}$	$^{+2.3}_{-0.2}$	1.28
1.0, 1.5	8.0	0.6	$^{+1.1}_{-0.3}$	$^{+0.9}_{-0.3}$	1.38

Table 3. Differential cross sections for the diffractive photoproduction of dijets as a function of x_{γ}^{obs} listed with statistical (δ_{stat}) and systematic (δ_{syst}) uncertainties and energy scale (δ_{ES}) uncertainties; the last column shows the hadronisation corrections applied to the NLO QCD predictions

x_{γ}^{obs} bin	$\frac{\mathrm{d}\sigma/\mathrm{d}x_{\gamma}^{\mathrm{obs}}}{\mathrm{(pb)}}$	$\delta_{ m stat} \ m (pb)$	$\delta_{ m syst} \ m (pb)$	$\delta_{\mathrm{ES}} \ \mathrm{(pb)}$	C_{had}
0.250, 0.375	28.5	2.4	$^{+1.4}_{-3.0}$	$^{+0.5}_{-1.1}$	1.23
0.375, 0.500	52.7	3.2	$^{+2.7}_{-4.1}$	$^{+4.2}_{-1.9}$	1.04
0.500, 0.625	78.1	3.7	$^{+3.2}_{-4.2}$	$^{+1.9}_{-4.5}$	1.01
0.625, 0.750	114.3	4.5	$^{+6.8}_{-7.4}$	$^{+5.9}_{-7.3}$	1.18
0.750, 1.000	356.5	6.2	$^{+29.1}_{-14.1}$	$^{+23.3}_{-14.4}$	1.07

tions, i.e. ratios of event yields at hadron level to those at parton level.

The MC generator RAPGAP [53] was used to simulate dijet processes in diffractive photoproduction at the Born level. Electroweak radiative effects were simulated by using RAPGAP in conjunction with HERACLES 4.6 [54].

The electron–proton interactions at small Q^2 were modelled with both direct and resolved photon processes (Fig. 1). Events were generated assuming that diffractive processes proceed via the emission of a particle-like pomeron from the proton followed by the interaction of the virtual photon with the pomeron. Although this factorised approach has no justification in QCD, it gives a fair description of the data. The diffractive PDFs, as determined by the H1 Collaboration (H1 LO fit 2) [55] for the pomeron contribution, were used. For resolved photon processes, the photon PDFs GRV-G-HO [56] were chosen.

In the simulation chain, the process of QCD radiation is followed by hadronisation. This was simulated by interfacing RAPGAP to a parton-shower model as implemented in MEPS [57] and to a hadronisation model based on string fragmentation [58, 59] as implemented in JETSET [60, 61].

The generated MC events were passed through the standard simulation of the ZEUS detector, based on the GEANT program [62], and a trigger-simulation package [48, 49]. The simulated events were reconstructed and selected in the same way as the data.

Since the MC events generated with RAPGAP did not adequately describe the $z_{I\!P}^{\rm obs}$ distribution of the data, they were reweighted to the measured distribution separately for $x_{\gamma}^{\rm obs} \geq 0.75$ and $x_{\gamma}^{\rm obs} < 0.75$. The relative fractions of direct photon and resolved photon processes were determined from a fit to the data. Resolved processes account for about one third of the total event sample.

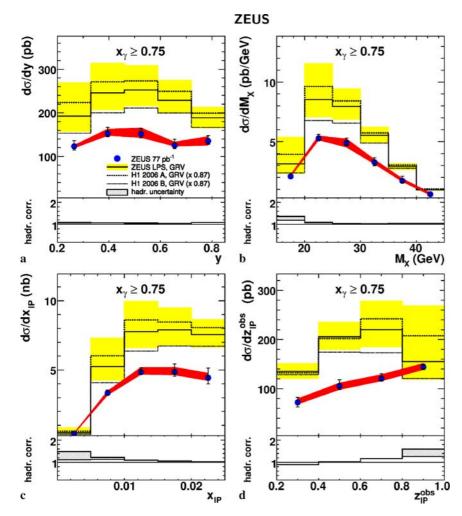


Fig. 5. Single-differential cross sections as a function of a y, b M_X , c x_{IP} and d $z_{IP}^{\rm obs}$ for direct-photon-enriched dijet photoproduction ($x_{\gamma}^{\rm obs} \geq 0.75$) compared with NLO QCD predictions, corrected for hadronisation, using the dPDFs from the ZEUS LPS fit ($solid\ line$), the H1 2006 fit A ($dashed\ line$) and the H1 fit B ($dotted\ line$) and the GRV γ -PDFs. Underneath each plot hadronisation corrections are shown which were obtained with RAPGAP ($upper\ histogram$) and POMWIG ($lower\ histogram$), respectively. The $shaded\ bands$ indicate the differences. The corrections from RAPGAP were applied to obtain the NLO predictions shown above. Further details are the same as in the caption of Fig. 3

Event distributions are compared with the reweighted RAPGAP MC distributions for the kinematic variables y, M_X , $E_{\rm T}^{\rm jet1,2}$ and $\eta^{\rm jet1,2}$ in Fig. 2. The MC distributions were normalised to the data yielding a reasonable overall description of the data.

The hadronisation corrections were calculated with the RAPGAP MC sample after reweighting its parton level z_{IP}^{obs} distribution to each of the NLO predictions described in Sect. 8.2. In addition, hadronisation corrections were also calculated with a MC sample generated with POMWIG [63], a modification of the HERWIG MC program [64] based on a cluster fragmentation model [65,66]. Since only direct photon interactions can be simulated with POMWIG, the comparison to RAPGAP was restricted to the range $x_{\gamma}^{\text{obs}} \geq 0.75$. The bin-by-bin differences between the corrections obtained with the two programs give an indication of the systematic uncertainties due to the hadronisation corrections [52].

The MC generator PYTHIA [67] was used to model the non-diffractive photoproduction of two jets. Events were generated using the CTEQ5L [68] (GRV-G-HO) parametrisation of the proton (photon) PDFs and processed through the same simulation and selection chain as the data.

6 Background

Background from proton-dissociative events, with a low-mass proton-dissociative system escaping down the beam pipe, was estimated to be $(16\pm4)\%$ [51] by fitting to the FPC energy distribution, without the $E_{\rm FPC}$ cut, a mixture of RAPGAP and EPSOFT MC [69]. This value was also obtained from hard diffractive production of open charm [70]. It was assumed that this estimate is independent of all kinematic variables studied here. The measured cross sections were scaled down accordingly.

Background from non-diffractive dijet photoproduction, as estimated with the PYTHIA MC, was found to be less than 5% throughout the whole kinematic range, and was neglected.

7 Systematic uncertainties

Systematic uncertainties on the measured cross sections were estimated as described below:

• the trigger efficiency was estimated for both data and Monte Carlo events using an independent trigger branch. The efficiency was above 98% for the entire kine-

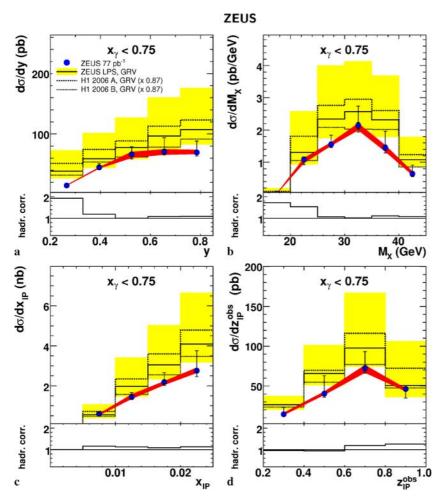


Fig. 6. Single-differential cross sections as a function of **a** y, **b** M_X , **c** x_{IP} and **d** $z_{IP}^{\rm obs}$ for resolved-photon-enriched dijet photoproduction ($x_{\gamma}^{\rm obs} < 0.75$) compared with NLO QCD predictions, corrected for hadronisation, using the dPDFs from the ZEUS LPS fit (solid line), the H1 2006 fit A (dashed line) and the H1 2006 fit B (dotted line) and the GRV γ -PDFs. Underneath each plot the hadronisation corrections applied to the NLO predictions at parton level are shown. Further details are the same as in the caption of Fig. 3

matic range. The Monte Carlo simulation agrees with the data within $\pm 1\%$ [52] and the uncertainty was neglected;

- the transverse jet-energy scale was varied by $\pm 3\%$, the typical uncertainty in this $E_{\rm T}^{\rm jet}$ range [28]. This variation resulted in an uncertainty of less than $\pm 5\%$;
- the FPC energy cut was varied by ± 0.5 GeV, resulting in an uncertainty less than $\pm 1\%$ in most bins and not more than $\pm 2\%$;
- changing the energy threshold of the EFOs, which is used to calculate $\eta_{\rm max}$, by $\pm 100\,{\rm MeV}$ led to an uncertainty typically less than $\pm 1\%$ and not more than $\pm 2\%$ in any bin;
- the η_{max} values of data and Monte Carlo events were shifted relative to each other by ± 0.1 , the typical η resolution. This led to the largest observed uncertainties which were typically below $\pm 6.5\%$ and up to $\pm 14\%$ for low $z_{I\!\!P}^{\text{obs}}$ and large $x_{I\!\!P}$ and M_X ;
- the lower $y_{\mathbb{J}\mathbb{B}}$ cut was varied within its resolution (0.04); the resulting uncertainties were typically less than $\pm 1\%$ and not more than $\pm 3\%$. When the higher $y_{\mathbb{J}\mathbb{B}}$ cut was lowered, the measured cross sections changed typically by < 1% and not more than $\pm 4\%$;
- varying the $\eta^{\rm jet}$ cuts within its resolution (0.1) gave an uncertainty which is mostly below $\pm 1\%$ and not more than $\pm 4\%$;

• the x_{IP} cut was varied within its resolution (0.0025); the resulting uncertainties were typically less than $\pm 2\%$, increasing to $\pm 6\%$ in the highest M_X and η^{jet1} bins.

The systematic uncertainties not associated with the jet-energy scale were added in quadrature to the statistical uncertainty and are shown as error bars of the measured cross sections in Figs. 3–6. The uncertainty due to the energy scale is shown separately as a shaded band in each of the figures. Overall normalisation uncertainties of $\pm 2.2\%$ from the luminosity determination and of $\pm 4\%$ from subtraction of the dissociative background were not included.

8 Results

8.1 Cross sections

Single-differential cross sections were measured in the kinematic region $Q^2 < 1 \, \mathrm{GeV^2}, \ 0.20 < y < 0.85, \ x_{I\!\!P} < 0.025, \ E_{\mathrm{T}}^{\mathrm{jet1(2)}} > 7.5 \, (6.5) \, \mathrm{GeV}$ and $-1.5 < \eta^{\mathrm{jet1,2}} < 1.5$, and were determined as a function of $y, \ M_X, \ x_{I\!\!P}, \ z_{I\!\!P}^{\mathrm{obs}}, \ E_{\mathrm{T}}^{\mathrm{jet1}}, \eta^{\mathrm{jet1}}$ and $x_{\gamma}^{\mathrm{obs}}$. The estimated contribution of proton-dissociative background of 16% was subtracted in all bins.

Table 4. Differential cross sections for the diffractive photoproduction of dijets for $x_{\gamma}^{\text{obs}} \geq 0.75$ listed with statistical (δ_{stat}) and systematic (δ_{syst}) uncertainties and energy scale (δ_{ES}) uncertainties; the last column shows the hadronisation corrections applied to the NLO QCD predictions

y bin	$d\sigma/dy$	δ_{stat}	δ_{syst}	δ_{ES}	$C_{ m had}$
	(pb)	(pb)	(pb)	(pb)	
0.20, 0.33	123.2	5.1	$^{+12.0}_{-6.7}$	$^{+2.3}_{-3.8}$	1.10
0.33, 0.46	152.6	5.7	$^{+13.0}_{-4.5}$	$^{+10.2}_{-4.8}$	1.07
0.46, 0.59	151.8	5.7	$^{+11.0}_{-7.3}$	$^{+13.6}_{-8.5}$	1.07
0.59, 0.72	125.2	5.0	$^{+13.4}_{-5.3}$	$^{+7.9}_{-1.8}$	1.05
0.72, 0.85	135.3	5.4	$^{+11.3}_{-4.9}$	$^{+10.6}_{-9.8}$	1.09
M_X bin	$\mathrm{d}\sigma/\mathrm{d}M_X$	$\delta_{ m stat}$	$\delta_{ m syst}$	δ_{ES}	$C_{ m had}$
(GeV)	(pb/GeV)	(pb/GeV)	(pb/GeV)	(pb/GeV)	
15.0, 20.0	2.08	0.11	$^{+0.10}_{-0.01}$	$^{+0.13}_{>-0.01}$	1.37
20.0, 25.0	5.27	0.16	$^{+0.30}_{-0.08}$	$^{+0.22}_{-0.13}$	1.11
25.0, 30.0	4.88	0.16	$^{+0.38}_{-0.17}$	$^{+0.35}_{-0.35}$	1.05
30.0, 35.0	3.26	0.14	$^{+0.36}_{-0.25}$	$^{+0.23}_{-0.14}$	1.03
35.0, 40.0	1.70	0.11	$^{+0.36}_{-0.16}$	$^{+0.19}_{-0.06}$	1.05
40.0, 45.0	0.58	0.07	$^{+0.12}_{-0.07}$	$^{+0.12}_{-0.07}$	1.05
x_{IP} bin	$\mathrm{d}\sigma/\mathrm{d}x_{I\!P}$	$\delta_{ m stat}$	$\delta_{ m syst}$	$\delta_{ m ES}$	C_{had}
	(nb)	(nb)	(nb)	(nb)	
0.000, 0.005	0.40	0.06	$^{+0.01}_{-0.05}$	$^{+0.03}_{>-0.01}$	1.48
0.005, 0.010	3.33	0.12	$+0.18 \\ -0.05$	$^{+0.14}_{-0.15}$	1.22
0.010, 0.015	4.84	0.15	$^{+0.27}_{-0.09}$	$^{+0.34}_{-0.16}$	1.10
0.015, 0.020	4.86	0.16	$^{+0.56}_{-0.26}$	$^{+0.34}_{-0.22}$	1.06
0.020, 0.025	4.43	0.18	$+0.68 \\ -0.40$	+0.34 -0.21	1.03
$z_{I\!P}^{ m obs}$ bin	$d\sigma/dz_{IP}^{\rm obs}$	$\delta_{ m stat}$	$\delta_{ m syst}$	$\delta_{ m ES}$	C_{had}
	(pb)	$(\mathrm{pb}/\mathrm{GeV})$	(pb/GeV)	(pb/GeV)	
0.2, 0.4	72.0	4.7	+9.1 -8.1	$+7.4 \\ -3.3$	0.89
0.4, 0.6	105.3	4.2	$^{+12.3}_{-5.6}$	$^{+6.5}_{-7.1}$	1.02
0.6, 0.8	120.6	3.8	$+9.5 \\ -3.1$	$^{+8.0}_{-4.8}$	1.17
0.8, 1.0	144.0	3.8	$^{+4.4}_{-2.4}$	$^{+7.3}_{-5.2}$	1.59

The cross sections are shown in Figs. 3 and 4 and listed in Tables 1–3. The cross section dependence on x_{γ}^{obs} , shown in Fig. 4, indicates that direct-enriched ($x_{\gamma}^{\text{obs}} \geq 0.75$) processes dominate diffractive dijet photoproduction in the kinematic range of this measurement.

Single-differential cross sections were also determined separately for direct-photon enriched and resolved-photon enriched processes. They are shown in Figs. 5 and 6, respectively, and listed in Tables 4 and 5. The two sets of distributions differ in shape. Typically, resolved events are characterised by larger diffractive masses M_X ; this in turn reflects into the observed x_{IP} behaviour. Slight differences are observed in the $z_{IP}^{\rm obs}$ distributions with the most prominent feature being the rise of the direct-enriched component when $z_{IP}^{\rm obs}$ approaches one.

8.2 Comparison to the NLO QCD calculations

NLO predictions for diffractive photoproduction of dijets were calculated at parton level with a program by Klasen and Kramer [71]. The calculations were performed with a fixed-flavour number of $N_{\rm f}=4$ and $A_4=330$ MeV, chosen to match the value of the running $\alpha_{\rm s}$ in the region of four active flavours. Three sets of dPDFs were used: the ZEUS LPS fit, determined from an NLO QCD fit to inclusive diffraction and diffractive charm-production data [8], and the H1 2006 fits A and B, obtained from fits to inclusive diffraction data [9]. The Regge-inspired parameters set for the NLO calculations were the same as used to obtain the dPDFs. The t-slope used in the pomeron flux was 5 GeV². For comparison with data, the NLO calculations

Table 5. Differential cross sections for the diffractive photoproduction of dijets for $x_{\gamma}^{\rm obs} < 0.75$ listed with statistical ($\delta_{\rm stat}$) and systematic ($\delta_{\rm syst}$) uncertainties and energy scale ($\delta_{\rm ES}$) uncertainties; the last column shows the hadronisation corrections applied to the NLO QCD predictions

y bin	$\frac{\mathrm{d}\sigma/\mathrm{d}y}{\mathrm{(pb)}}$	$\delta_{ m stat} \ m (pb)$	$\delta_{ m syst} \ m (pb)$	$\delta_{ m ES} \ m (pb)$	C_{had}
0.20, 0.33	14.7	1.5	+2.5	+0.7	1.93
*	44.9	$\frac{1.5}{2.7}$	$^{-1.0}_{+5.6}$	$-0.1 \\ +0.1$	1.93 1.19
0.33, 0.46			$-2.7 \\ +11.9$	$-1.7 \\ +3.9$	
0.46, 0.59	66.5	3.5	$-6.9 \\ +22.4$	$-5.9 \\ +3.6$	1.01
0.59, 0.72	71.0	3.6	$-4.4 \\ +18.6$	$-5.0 \\ +4.3$	1.08
0.72, 0.85	69.5	3.5	-4.5	-2.8	1.09
$\overline{M_X \text{ bin}}$	$\mathrm{d}\sigma/\mathrm{d}M_X$	$\delta_{ m stat}$	$\delta_{ m syst}$	$\delta_{ m ES}$	C_{had}
(GeV)	(pb/GeV)	(pb/GeV)	(pb/GeV)	$(\mathrm{pb}/\overline{\mathrm{GeV}})$	naa
15.0, 20.0	0.03	0.01	$^{+0.01}_{-0.01}$	$<+0.01 \\ >-0.01$	1.72
20.0, 25.0	1.09	0.07	$ \begin{array}{r} -0.01 \\ <+0.01 \\ -0.15 \end{array} $	+0.04 -0.11	1.54
25.0, 30.0	1.55	0.07	$-0.13 \\ +0.27 \\ -0.07$	$^{-0.11}_{+0.06}_{-0.04}$	1.07
30.0, 35.0	2.14	0.10	+0.59	+0.07	1.01
35.0, 40.0	1.45	0.09	$-0.18 \\ +0.50 \\ 0.14$	$-0.14 \\ +0.07 \\ 0.10$	1.11
40.0, 45.0	0.64	0.06	$-0.14 \\ +0.26 \\ -0.06$	$^{-0.12}_{+0.07}_{-0.04}$	1.08
x_{IP} bin	$\mathrm{d}\sigma/\mathrm{d}x_{IP}$	$\delta_{ m stat}$	$\delta_{ m syst}$	δ_{ES}	$C_{ m had}$
x IP bili	(nb)	(nb)	(nb)	(nb)	\circ_{had}
0.005, 0.010	0.60	0.05	<+0.01 -0.07	<+0.01 -0.07	1.16
0.010, 0.015	1.44	0.08	-0.07 + 0.20 -0.09	$^{-0.07}_{+0.13}_{-0.08}$	1.13
0.015, 0.020	2.19	0.10	+0.46	+0.04	1.08
0.020, 0.025	2.76	0.12	$-0.13 \\ +0.99 \\ -0.28$	$-0.14 \\ +0.15 \\ -0.11$	1.13
z_{IP}^{obs} bin	$\mathrm{d}\sigma/\mathrm{d}z_{IP}^{\mathrm{obs}}$	$\delta_{ m stat}$	$\delta_{ m syst}$	δ_{ES}	$C_{ m had}$
~IP biii	(pb)	(pb)	(pb)	(pb)	∨had
0.2, 0.4	14.4	1.8	$+8.5 \\ -1.5$	$^{+1.8}_{-0.9}$	0.96
0.4, 0.6	40.4	2.6	$^{-1.3}_{+22.3}_{-3.7}$	$^{-0.9}_{+2.5}_{-1.4}$	0.95
0.6, 0.8	72.3	3.1	+20.7	+3.8	1.19
0.8, 1.0	46.2	1.8	$^{-5.6}_{+0.8}_{-11.3}$	$-5.5 \\ +0.8 \\ -2.7$	1.26

obtained with the H1 dPDFs were scaled down by a factor of 0.87 [9]. The contribution of subleading Regge trajectories as implemented in the H1 fits was included. For the resolved photon, the γ -PDF parametrisations GRV [56] and AFG04 [72] were used.

The NLO QCD predictions were obtained setting the renormalisation and factorisation scales to $\mu_{\rm R}=\mu_{\rm F}=\mu=E_{\rm T}^{\rm jet1}$. The theoretical uncertainties were estimated by varying the scales simultaneously between $(0.5 \cdot E_{\rm T}^{\rm jet1})$ and $(2 \cdot E_{\rm T}^{\rm jet1})$ [71]. Changing the number of active flavours to $N_{\rm f}=5$ in the NLO calculations leads to an increase of the expected cross section for $x_{\gamma}^{\rm obs} \geq 0.75$ by less than 10%, and to a negligible effect elsewhere. The uncertainties of

the dPDFs and the pomeron flux, constraining directly the normalisation, were not included. The predicted cross sections were transformed to the hadron level using the hadronisation corrections calculated with RAPGAP as described in Sect. 5. The uncertainties of the hadronisation corrections are not included in the error calculations for the cross sections.

The data are compared with NLO QCD predictions at hadron level for the full $x_{\gamma}^{\rm obs}$ range in Figs. 3 and 4. The hadronisation corrections applied to the NLO predictions at parton level are shown in the lower part of each plot and the values are given in Tables 1–3. The asymmetric theoretical uncertainties, estimated as described, were determined for the ZEUS LPS fit; those for the other NLO predictions are similar. The data are reasonably well described in shape. However, they lie systematically below all the predictions. Most of the suppression originates from the lower $E_{\rm T}^{\rm jet1}$ region.

 $^{^3}$ The H1 measurements used to derive the H1 dPDFs include low-mass proton-dissociative processes which leads to an overestimate of the photon-diffractive cross section by a factor of $(1.15^{+0.15}_{-0.08})$ as obtained from MC simulations [9].

Figure 4b shows the ratio of the data and the NLO predictions using the ZEUS LPS fit. The ratio is below one, consistent with a suppression factor of about 0.7 independent of x_{γ} . Also shown is the ratio expected if the calculated resolved-photon cross section is suppressed by a factor of 0.34 [25, 26]. No additional suppression factor for resolved-enriched data is observed. The suppression factor depends on the dPDFs and ranges between about 0.6 (H1 2006 fit A) and about 0.9 (H1 2006 fit B). Within the large uncertainties of NLO calculations, the data are compatible with no suppression, as expected in [27].

Differential cross sections for the direct-enriched and resolved-enriched samples are compared with NLO predictions at hadron level in Figs. 5 and 6. Again the hadronisation corrections are shown in the lower part of each plot and the values are given in Tables 4 and 5. For direct-enriched data, the hadronisation corrections are shown for both RAPGAP and POMWIG. The differences are taken as an estimate of the uncertainties as described in Sect. 5. The data lie systematically below the NLO calculations. Also, contrary to NLO expectations, the cross section as a function of $z_{IP}^{\rm obs}$ for the direct-enriched sample rises steadily with increasing $z_{IP}^{\rm obs}$.

Compared to NLO calculations obtained with the program of Frixione and Ridolfi [73], the H1 Collaboration observed a suppression factor of about 0.5 in both resolved-enriched and direct-enriched cross sections of diffractive dijet photoproduction [13]. The measurements of ZEUS and H1 cover different kinematic regions in $E_{\rm T}$ and x_{IP} . In particular, the H1 measurements extend to lower $E_{\rm T}$ values than in the ZEUS analysis. In ZEUS, the largest discrepancy between the measured and predicted values of the cross section is observed at the lowest $E_{\rm T}$ values suggesting that the conclusion on factorisation breaking depends on the probed scale.

9 Conclusions

Cross sections for diffractive photoproduction of dijets were measured with the ZEUS detector at HERA using an integrated luminosity of 77.2 pb $^{-1}$. The measurements were performed in the kinematic region $Q^2<1~{\rm GeV^2},$ 0.20< y<0.85 and $x_{I\!P}<0.025.$ The two jets with highest transverse energy were required to have $E_{\rm T}^{\rm jet1(2)}>7.5~(6.5)~{\rm GeV}$ and $-1.5<\eta^{\rm jet1,2}<1.5.$

The measured differential cross sections are compared to NLO QCD predictions based on available parameterisations of diffractive PDFs. The comparisons were made for the full data sample as well as for the subsamples enriched with resolved photon ($x_{\gamma}^{\rm obs} < 0.75$) and direct photon ($x_{\gamma}^{\rm obs} \ge 0.75$) processes. The NLO calculations tend to overestimate the measured cross sections of both the resolved-enriched and the direct-enriched data sample. However, within the large uncertainties of the NLO calculations the data are compatible with QCD factorisation.

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